CALCULATING LOADABILITY LIMITS OF DISTANCE RELAYS

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Introduction

Typically, distance relays protect transmission lines from power system faults by using the method of step distance protection. This method uses the line impedance as the basis to form zones of protection and each zone is calculated by a predetermined percentage of the line impendence. The impedance setting will establish the relay's impedance characteristic, which is graphically displayed as circles or quadrilaterals in the R-X plane. A distance relay is capable of detecting faults, indicated by a drop in the impedance of the line, when the observed impedance is inside the relay's defined impedance characteristic.

The load flowing through a transmission line also appears as impedance to the distance relay, and is typically called "load impedance". As the power load on the transmission line increases, the load impedance decreases, and as the power load of the transmission line decreases, the load impedance increases. During steady-state or normal conditions, the load impedance is large enough that it remains far enough from the relay's characteristic shape. In some situations, however, the power load of the line is sufficiently large that it reduces the load impedance to a point which encroaches on the relay's characteristic shape. As a result, the distance relay identifies the encroachment as a fault and consequently trips the line out of service. This is a highly undesirable operation because a heavily loaded line has been taken out of service when no real fault exists.

Over the years, different methods have been used in order to avoid problems with load encroachment, and each method presents its advantages and disadvantages. Regardless of the method used, each relay will have a maximum "loadability limit" that will cause the relay to operate under high load conditions. Therefore, it is important for the relay engineer to understand and take time to calculate the maximum loadability limits of the relay so as to avoid settings that will be susceptible to load encroachments.

This technical document focuses on concepts, definitions and calculation on how to find the maximum loadability limit of a distance relay with mho and lens characteristics.

Apparent Impedance and Power Quantities

A distance relay measures the voltages and currents provided by a transmission line's instrument transformers. Then, the current and voltage phasor representation is obtained and its sequences components are calculated at the relay location. The positive sequence impedance is then calculated using the positive sequence voltage and current values. The measured or apparent impedance can be plotted in the R-X diagram and checked to see whether the impedance is inside one of zones of protection. Although the apparent impedance is not a good way to detect faults due to load flow and fault resistance conditions, it is a good way to detect load conditions [6]. At any given load, the apparent impedance values seen by the relay can fluctuate depending on the state of the line load, and impedance values can vary.

In some instances, such as high line loads and power swing conditions, the fluctuation of voltage and current may cause the load impedance to overlay or penetrate on the zone protection characteristics (mho, quad) and; therefore, reach the maximum loadability limit of the relay, thereby causing an undesired tripping operation. It is important, therefore, to know the limit of the relay for different types of load conditions. However, we must first understand the relationships and characteristics that are experienced between the load of the line and its impedance.

Since relays measure voltage and current values, the power factor can also be calculated. As a result, apparent (S), real (P) and reactive (Q) power can be derived from current and voltage measurements. The three phase and per phase relationships between the voltage (V), current (I), impedance (Z) and power are given by the following formulas:

$$S3\emptyset = \overline{3} * VLL * IL$$
$$IL = \frac{S3\emptyset}{\overline{3} * VLL}$$

$$P3\phi = \overline{3} * VLL * IL * Cos \ \theta v - \theta i$$

$$Q3\phi = \overline{3} * VLL * IL * Sin \ \theta v - \theta i$$

$$P1\phi = VLN * IL * Cos \ \theta v - \theta i \ Watts$$

$$Q1\phi = VLN * IL * Sin(\theta v - \theta i) \ Vars$$

$$S\phi = (VLN * IL^*) \ VA$$

$$Z = \frac{VLN}{IL}$$

R-X and **P-Q** Relationships

The power delivered by a transmission line is usually given as real (MWs) power, reactive (MVARs) power, and apparent (MVA) power. We can then use these values to calculate the R and X coordinates and represent the same three-phase balance system in the R-X diagram. The relationship between the three power quantities with R and X is given below.

$$R = \frac{VLN^2 * P10^2}{P10^2 + Q10^2}$$
$$X = \frac{VLN^2 * Q10^2}{P10^2 + Q10^2}$$

The position for the R and X coordinates in the R-X plane depends on the direction of power and the power factor. For example, consider the oneline diagram shown in **Figure 1**.



Figure 1. Three Bus System-Oneline Diagram

If the direction of real and reactive power is from bus 1 to bus 2, the R-X coordinates are located in quadrant I. If the direction of real power is from bus 1 to bus 2 and the reactive power is from bus 2 to bus 1, then the R-X coordinates are located in quadrant IV. **Figure 2** shows the P-Q and R-X relationships for all four quadrants.



Figure 2. R-X Diagram and Power Flow Direction

We can observe from **Figure 2** that unity power factor is achieved when the value of jX equals zero. This means that the system is purely resistive and that the current and voltage waveforms are in phase. In a real power system, a unity power factor is not practical; a power factor lower than 1 is found due to the capacitive and reactive elements. For most power systems, the power factor angles range from zero to +/-40 degrees [1]. This means that the R-X values calculated from the P-Q values are bounded by the power factor angle (Θ). This is shown in **Figure 3**.



Figure 3. R-X Diagram, Power Flow Direction and Power Factor

The shaded area represents the apparent load impedance, and it can be seen that the line load impedance can occur in any of the four quadrants. In order to emphasize these concepts even further, **Table 1** shows the R and jX sign convention in conjunction with leading and lagging power factors [2].

Table	1.	Sign	Conv	ention	for	R	and	iX
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Condition	Sign of R	Sign of jX
Power Flow from Bus 1 to 2	Positve (+)	
Power Flow from Bus 2 to1	Negative (-)	
Lagging Reactive Power from Bus 1 to 2		Positive (+)
Lagging Reactive Power from Bus 2 to 1		Negative (-)
Leading Reactive Power from Bus 1 to 2		Negative (-)
Leading Reactive Power from Bus 2 to 1		Positive (+)

Example:

Let's consider the system shown in **Figure 4**, which has the following data:



Figure 4. Line 1 Oneline Diagram

 $\begin{array}{l} V1 = 138 \angle 0^{\circ} \ kV = VLN = 76.6 \angle 0^{\circ} \ kV \\ V2 = 138 \angle 30^{\circ} \ kV = VLN = 79.6 \ \angle 30^{\circ} = (69 + j39.8) \ kV \\ ZLine = 66 \angle 75^{\circ} \ \Omega = (17.08 + j63.75) \ \Omega \end{array}$

Using Kirchhoff's Law, we have:

 $-76.6kV + I \ 66\angle 75^{\circ} \ \Omega + 79.6 \ \angle 30^{\circ} = kV = 0$ $I = -552.42 - j268.24 \ Amps$ $I = 614\angle - 154 \ Amps$

Calculating the Apparent Power (S) we have:

 $S@Bus1 = VLN * IL^*$

 $S@Bus1 = 76.6kV * (-552.42 - j268.24 Amps)^*$

Taking the conjugate, we have:

$$S@Bus1 = 76.6kV * -552.42 + j268.24$$
 Amps
 $S@Bus1 = -42.3 + j20.5$ MVA
 $S@Bus1 = 47.04 \angle 154^{\circ}$ MVA

Since S = P + jQ:

$$S@Bus1 = -42.3MWs + j20.5MVars$$

From the relay reference, the results indicate that real power is flowing from bus 2 to 1 and that the reactive power is flowing from bus 1 to 2.

Let's now translate these values to R and jX. We know that:

$$S = VLN * IL^{*}$$
$$IL^{*} = \frac{VLN}{Z}$$
$$S = VLN * \frac{VLN}{Z} * = VLN * \frac{VLN^{*}}{Z^{*}}$$
$$VLN = VLN e^{(j\theta v - \theta i)}$$
$$VLN^{*} = VLN e^{-j(\theta v - \theta i)}$$
$$Z^{*} = Z e^{-j(\theta v - \theta i)}$$

Therefore:

$$S = \frac{VLN * VLN e^{j\theta - j\theta}}{Z e^{-j(\theta v - \theta i)}} = \frac{VLN^2 e^{j(\theta v - \theta i)}}{Z}$$

Calculating for Z:

$$Z = \frac{76.6kV^2 \cos 154^\circ + j \sin 154^\circ}{47.04 \text{ MVA}}$$
$$Z = -112.11 + j54.68 = 124 \angle 154^\circ \text{ Ohms}$$

The load impedance has a negative R value and a positive jX value, and those coordinates are located in quadrant II, as indicated in **Figure 4**. This example has demonstrated that the location of the load impedance depends on the direction of power. This concept will be emphasized even further when we calculate the maximum loadability of the relay for different power factor conditions.

Line, Load and Relay Impedances

Transmission lines are usually protected by step distance protection using the mho or quadrilateral relay characteristic with three or four zones of protection. Each zone of protection is based on a percentage of the line impedance, which varies depending on the philosophy and criteria of each utility. However, zone 1 is usually 80%, zone 2 is 120% and zone 3 is 150% of the protected line impedance. Some relay manufacturers use zone 3 in the reverse direction, but for this application, zone 3 will be in the forward direction.

Figure 5 shows a one-line diagram with a distance relay protecting Line 1. The diagram also shows the difference in distance for each zone of protection. If we use these criteria for each of the zones' coverage areas, we have the following:





Figure 5. Step Distance Protection

The R-X diagram is one of the best tools a relay engineer can use to visualize the location and behavior of the impedances. As a result, we can plot the line, load and relay impedances in the R-X plane to better visualize their location and proximity to each other. We will see how this can be done in the following sections.

Line Impedance - ZLine

The ZLine is the positive sequence primary phase-to-neutral line impedance. In a 60 HZ system, the impedance is about 0.8 ohms per mile. The angle (α) of this impedance depends on the conductor size and spacing, but generally it is in the range of 65-85 degrees for an overhead line [5]. The line impedance is plotted in the R-X diagram as shown in **Figure 6**. Once plotted, we can easily observe that the line R+jX components can be derived by the familiar relationships:

 $R = ZLine * Cos \alpha$ and $jX = ZLine * Sin \alpha$



Figure 6. Line Impedance

Load Impedance - ZLoad

As we discovered during the R-X and P-Q relationship section, the position of the load impedance in the R-X diagram depends on the direction of power. If we assume that the real and reactive power flows from bus 1 to 2, then the load impedance will be located in the first quadrant of the R-X plane. We also know that the load impedance region is bounded by the power factor angle, which usually has a value of 0 to +/-40 degrees. In our previous example, we found out that the load impedance value was located in the second quadrant of the R-X plane since:

$$Zload = -112.11 + j54.68 = 124 \angle 154^{\circ} Ohms$$

For the purpose of simplification and explanation, let's assume that the real power is in the direction from bus 1 to 2, which will put the load impedance in the first quadrant. In this case, we will have:

$$ZLoad = 112.11 + j54.68 = 124 \angle 26 Ohms$$

Figure 7 shows the relationships between the line and load impedances with their respective angles superimposed in the R-X diagram.



Figure 7. Line and Load Impedances

Relay Impedances - Zr:

The relay impedances are the values that a distance relay uses for zones of protection. These values (settings) can be used with different types of relay characteristics, such as the mho, lens, tomato and quadrilateral. These relay characteristics form different shapes in the R-X diagram that allow for many different types of applications. Even though there are many different types of relay characteristics, the mho circle is the most common. Using the values for each zone of protection from **Figure 5** and Line 1, the mho characteristics for each zone are shown in **Figure 8**. We can observe that the diameter of each mho circle is based on the value of each zone of protection. In addition, the load impedance has been superimposed in the R-X plane with the mho circles in order to better visualize its locations.

We know that during steady-state or normal system conditions, the load impedance remains constant and is high enough to keep it away from the relay zones of protection. From the graph, we can also see that the relay will trip as soon as the load impedance touches the outermost mho circle. So we must ask ourselves, "what is the maximum power that the line can transport that causes the load impedance to touch or encroach into the outermost mho circle?". In the next section, we will learn how to calculate these values.



Figure 8. Line 1 Relay mho Characteristics

Distance Relays Characteristics and Loadability Limits

The maximum loadability limit of a transmission line or conductor is bounded by the maximum current such conductors can carry before the conductor anneals and losses its elasticity. In most cases, calculations are performed that limit the amount of power a particular conductor can carry before the annealing point. A transmission line conductor's rating is based on static and dynamic properties that vary depending on the amount of load and ambient temperature. These ratings provide the operating and planning engineers with continuous, long-term and short-term emergency ratings. The short-term emergency rating will be the highest rating at which a transmission line conductor can be operated. The maximum ratings at which a particular line is operated have a direct impact on the maximum loadability limit of a distance relay.

In previous sections, we have shown that the power load (MVA) of a particular line can be converted into R-X values as load impedance. If the load of a line is high enough, it is possible that the load impedance may encroach into one of the mho circles. This is because as load increases, the load apparent impedance decreases, moving it closer to the origin [1]. This can be seen in **Figure 9**.

We can see that during low load conditions, the load impedance is located farther from the mho circle and the R-X origin. However, when load conditions are high, the load impedance moves toward the origin until a tripping point is reached when the load impedance equals the maximum loadability of the relay, at a given power factor. Relay engineers must ensure that a distance relay does not trip under high load conditions in order to give system operators time to mitigate system problems. Therefore, a relay engineer must be able to calculate the relay loadability limits for different distance relay characteristics and power factor angles, which is the focus of next section. First, however, we must understand the elements of a mho circle.



Figure 9. R-X Diagram, Supperimposed mho Circle and Loadability Limits

The mho Circle

The mho circle one is the most used relay characteristic for step distance protection. For this reason, we will put more emphasis on this type rather than others such as quadrilateral characteristics. The mho circle is composed of its impedance maximum reach, maximum torque angle and relay characteristic angle.

<u>Impedance Maximum Reach</u>: The mho circle maximum reach is set by the impedance reach Zr of the protective zone. As explained previously, these impedance reaches vary depending on the zone of protection such as zone 1, 2, 3 and 4. Each impedance value determines the diameter of the mho circle.

<u>Maximum Torque Angle (MTA)</u>: The angle of maximum torque of a distance relay using the mho characteristic is the angle at which it has the maximum reach. For microprocessor relays, the MTA is the same as the positive sequence line impedance angle. The MTA or line impedance angle varies depending on the voltage level of the transmission line. For example, in the extra high voltage or EHV transmission lines, the angles are higher and for lower voltage transmission and sub-transmission systems, the angles tend to be lower because the ratio of reactance to resistance is usually lower [4].



Figure 10. mho Circle Characteristic

<u>Relay Characteristic Angle:</u> The relay characteristic angle (RCA) of a mho circle is 90°. For purposes of calculating the maximum relay loadability, the RCA is the angle whose vertices are made between the load impedance vector and the difference between the line impedance and load impedance vectors. The circular shape is formed when the Zr vector and the RCA are fixed quantities. As the Zload vector increases with higher power factors, the Zr-Zload vector decreases, resulting in a locus that forms a circle. This is shown in **Figure 10**.

From here, we can calculate the load impedance value for the points on the circle by varying the value of the power factor. Once the load impendence value is known for such points in the circle, the MVA value will be known, which will indicate the maximum MVA value at which the relay will trip.

Calculating the Maximum Loadability of a Distance Relay with mho Characteristics

The relay impedances zones of protection must be selected carefully in order to avoid load encroachment problems. The zone of protection with greater risk is zone 3, since it is the mho circle with the greatest area and closest proximity to the load impedance. Zone 3 settings are certainly vulnerable to load encroachment conditions during high load and power swings conditions, which can cause the load impedance to travel towards the boundaries of the zone 3 mho circle and cause an undesired trip.

Since we now understand the basic principles that are associated with load impedances and mho circles, the calculation of the maximum relay loadability can now be performed. Since zone 3 is the zone with greatest risk of load encroachment, we will use zone 3 for our example.

From our Line 1 example shown in **Figure 5**, zone 3 has a value of $100 \angle 75^{\circ}\Omega$ primary. We want to know the maximum relay loadability that zone 3 will experience at different power factors. This is calculated in the steps below by using **Figure 11**.

- 1. Draw the zone 3 impedance vector in the R-X diagram.
- 2. Draw the load impedance vector at a specified power factor. For this example, $\theta = 30^{\circ}$.
- 3. Draw a right triangle forming the 90 ° relay characteristic between the load impedance vector and the difference vector that is made up of Z3 Zload. This is shown in Figure 11.



Figure 11. Maximum Relay Loadability Limits- mho Shape

4. Calculate the interior angle β that is made between the load and line impedance vectors. This is done by subtracting the line impedance angle minus the power factor angle.

$$\angle \beta = \angle \alpha - \angle \theta$$

$$\angle \beta = 75^{\circ} - 30^{\circ} = 45^{\circ}$$

5. Calculate the load impedance that the relay will experience at the specified power factor using right triangle properties:

$$Cos\beta = \frac{Zload}{Z3}$$

$$Zload, relay = 100 * Cos 45^{\circ} = 70.71 \angle 30^{\circ} \Omega$$

6. Calculate the maximum loadability of the relay in MVA by:

$$SRelay = \frac{kVLL^{2}}{Zload^{*}}$$
$$SRelay = \frac{138kV^{2}}{70.71\angle - 30^{\circ} \Omega^{*}}$$
$$SRelay = 269\angle 30^{\circ}MVA$$

Since S = P + jQ

$$SRelay = 233 MW + j134MVARs$$

7. Follow the same procedure and calculate the maximum loadability of the relay for different power factor angles as shown in **Table 2**. We can see that at a unity power factor, 734 MWs of power are necessary to trip the line with no reactive power. At a power factor of 90 °, 197 MVARs are necessary to trip the line with no real power. As the power angle increases to 120°, we see that the power flow direction has changed. Real power now runs from bus 2 to 1, and a real power of 190 MWs and reactive power of 329 MWs are necessary to trip the line.

Table 2. Relay Loadability 1	Limits for Different Power Factors
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Power Factor Θ	S (MVA)	P (MWs)	Q (MVARs)
0°	734	734	0
15°	378	365	97
30°	269	233	134
45°	219	154	154
60°	197	99	170
75°	190	49	183
90°	197	0	197
120°	380	-190	329

8. It is convenient to plot the MVA loadability limit values in the P-Q diagram to distinguish trip vs. no trip areas. This plot is shown in **Figure 12**, which emphasizes the amount of real and reactive power needed to trip a line based on zone 3 settings at different power factors.



Figure 12. P-Q Diagram and Loadability Limits

It can be observed from **Table 2** and extrapolated from **Figure 12** that for Line 1, operating at unity power factor, 734 MWs are required to trip.

Calculating the Maximum Loadability of a Distance Relay with Lens Characteristics

It might be necessary to change the characteristic shape of the impedance tripping zone to a lens shape. The lens characteristic reduces the zone coverage and therefore increases the amount of permissible load. However, relay engineers must keep in mind that by reducing the impedance coverage, the amount of coverage for resistive type faults is reduced.

The lens shape has a relay characteristic angle (RCA) that is in the range of $90^{\circ} > \theta > 120^{\circ}$. As the RCA increases, the impedance coverage area is reduced due to a narrower lens shape. In a similar manner, as with the mho circle characteristic with a RCA of 90° , we can calculate the maximum loadability in (MVA) of a distance relay that uses a lens characteristic.

As with the mho circle characteristic example, we will choose zone 3 for our calculations since this is the area of coverage with a greater risk to load encroachment.

The loadability is calculated as follows:

- 1. Draw the zone 3 impedance vector in the R-X diagram.
- 2. Draw the load impedance vector at a specified power factor. For this example, $\theta = 30^{\circ}$.
- 3. Choose a lens characteristic angle. This angle is formed between the load impedance vector and the difference between the zone 3 impedance and load impedance vectors. This is shown in **Figure 13**. A lenticular shape is formed when the lens characteristic angle and zone 3 impedance vector are fixed quantities. The lenticular locus is formed when the load impedance vector changes as the power factor angle changes. For this example, the lens characteristic angle $\varphi = 120^{\circ}$.



Figure 13. Maximum Relay Loadability and Lens Shape

4. Separate the inside triangle from the lens shape as shown in **Figure 14**. This allows us to see our impedance vectors and angles more clearly.



Figure 14. Applying the Law of Sines to Find the Load Impedance

5. Calculate the internal angle β .

6. Calculate the internal angles δ .

$$\angle \beta = \angle \alpha - \angle \theta$$
$$\angle \beta = \angle 75^{\circ} - \angle 30^{\circ} = 45^{\circ}$$
$$180^{\circ} = \angle \delta + \angle \varphi + \angle \theta$$
$$\angle \delta = 180^{\circ} - \angle \varphi - \angle \theta$$
$$\angle \delta = 180 - 120 - 45 = 15^{\circ}$$

7. Calculate the load impedance vector (ZLoad) by using the Law of Sines. See Figure 14.

$$\frac{a}{Sin(a)} = \frac{b}{Sin(b)}$$

$$\frac{Zload}{Sin(15)} = \frac{Z3}{Sin(120)}$$
$$Zload, R = \frac{100 * Sin(15)}{Sin(120)}$$
$$Zload, R = 30.0 \neq 30^{\circ} \Omega$$

8. Calculate the maximum loadability of the relay at the calculated load impedance and specified power factor of 30°.

 $S = \frac{kVLL^2}{Zload^*}$ $S = \frac{138kV^2}{30.0 \ \angle -30^\circ}$ $S = 634 \ \angle 30^\circ MVA$ S = 550 MWs + j317 KVARs

We can observe that by using the Lenticular characteristic, the amount of permitted load has been increased significantly compared to the mho characteristic with a value of 269MVA. The reader is encouraged to perform a P-Q diagram as in the previous section to determine the tripping area of the relay for different power factor values.

NERC Considerations

Following the blackout of August 2003, NERC has issued several considerations and documents that provide different guidelines that address zone 3 settings of distance relays and load encroachment. For example, NERC PRC - 023 recommends evaluating relay loadability at 0.85 p.u. voltage and a power factor angle of 30°. When these recommendations are used, the relay loadability limit is reduced from the values calculated in this document. As a result, the reader is encouraged to follow NERC standards when performing load encroachment calculations. In addition, the reader is advised to read the reference materials that cover this subject in more depth, and to learn about additional considerations that the relay engineer must be aware of before setting or employing load encroachment functions.

Conclusion

The loadability limits of distance relays are one of the most critical aspects of distance protection. This technical paper has presented the reader with valuable concepts on how to calculate the loadability limits of a distance relay and clarifies a lot of the ambiguity provided by current literature. The relay engineer should now be able to follow the steps on this paper along with NERC recommendations and be able to verify load encroachment problems before distance relay settings are applied.

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